

UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN
Department of Electrical and Computer Engineering

ECE 498DLJ PRINCIPLES OF SIGNAL ANALYSIS
Fall 2011

MIDTERM EXAM

Friday, October 21, 2011

- This is a **CLOSED BOOK** exam.
- There are a total of 100 points in the exam. Each problem specifies its point total. Plan your work accordingly.
- You must **SHOW YOUR WORK** to get full credit.

Problem	Score
1	
2	
3	
4	
5	
Total	

Name: _____

Problem 1 (20 points)

Calculate the Fourier series coefficients a_0 , a_k , b_k , $k = 1, 2, \dots$, for the periodic signal $x(t) = x(t + 8)$:

$$x(t) = \begin{cases} 1, & 0 \leq t < 1 \\ -1, & 1 \leq t \leq 3 \\ 0, & 3 < t < 8 \end{cases}$$

Problem 2 (20 points)

Compute the Fourier transform of $y(t)$. Write your answer in the form $Y(\Omega) = jA(\Omega)$, for some real-valued function $A(\Omega)$. The function $A(\Omega)$ should have no complex exponentials in it, and no imaginary parts.

$$y(t) = \begin{cases} 0.25, & -1 \leq t < 0 \\ -0.25, & 0 \leq t < 1 \\ 0, & \text{elsewhere} \end{cases}$$

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Problem 3 (20 points)

Start with the signal $x[n] = \delta[n] + \delta[n - 1]$. Find the 4-point DFT, $X[k]$, for $0 \leq k \leq 3$. Simplify, so that there are no complex exponentials left in your answer.

Problem 5 (20 points)

Assume that $x[n] = x_c(nT)$, where $1/T = 10,000$ samples/second. For each of the following signals, find $x[n]$ and $X_d(\omega)$.

(a) $x_c(t) = 0.2\text{sinc}(2000\pi t)$ (sinc, not sin!)

(b) $y_c(t) = \cos(7000\pi t)$.